

Answers to final exam NYB Fall 2013

1. a) $\frac{2x}{\sqrt{9+4x^2}}$ b) $\frac{1}{2}\sqrt{9+4x^2} + c$ 2. a) $\frac{3}{2}\ln|2x-1| + 2\ln(x^2+1) - 5\arctan x + c$

b) $-\frac{1}{4}\arccos^2(2x) \Big|_0^{1/4} = \frac{5\pi^2}{144}$ c) $\frac{1}{2}[x^4 \sin(x^2) + 2x^2 \cos(x^2) - 2\sin(x^2)] + c$

d) $-\frac{1}{5}\left[\ln|\cos(5x)| - \frac{\cos^2(5x)}{2}\right] + c$ e) $-\frac{1}{3}\left(\frac{\sqrt{1-x^2}}{x}\right)^3 + c$

3. a) $\lim_{x \rightarrow \infty} \frac{1}{2}\arctan\left(\frac{x-5}{2}\right) \Big|_5^x = \frac{\pi}{4}$ b) $\lim_{x \rightarrow 0^+} 2\sqrt{\tan x} \Big|_x^{\pi/4} = 2$

4. a) $-\frac{1}{3}$ b) e^{-2} c) $\frac{2}{5}$

5. $\frac{4}{3} \text{ units}^2$ 6. a) $2\pi \int_0^{3/2} x(-x^2 + 3x - x^2) dx$ b) $\pi \int_0^{3/2} (1+3x-x^2)^2 - (1+x^2)^2 dx$

7. $2\ln\left(\frac{(2+\sqrt{2})\sqrt{3}}{3\sqrt{2}}\right)$ 8. $y = \frac{3}{2} - \frac{1}{2x^2}$ 9. conv. to $\frac{3\pi}{2}$

10. a) conv. by comp.test or integral test b) conv. by ratio.test
c) conv. by Root.test d) Div. by Divergence test

11.a) conv. by Alternating series test and div. by Limit Comparison test. So it is conditionally convergent.

b) Absolutely Conv. By Ratio test

12. a) conv. telescoping sum $= -\frac{\pi}{6}$ b) Geometric conv. sum $= \frac{1}{3}$

13.a) Conv. b) we can not say anything about this series as x=5 might be the other end point of interval of convergence c)Conv. d)Div.

14. $R = \frac{1}{9}$ and the interval $\frac{17}{9} < x \leq \frac{19}{9}$

15.a) $-\frac{1}{3} + \frac{1}{9}\frac{(x-5)}{1!} - \frac{2}{27}\frac{(x-5)^2}{2!} + \frac{6}{81}\frac{(x-5)^3}{3!} - \frac{24}{243}\frac{(x-5)^4}{4!}$

b) $-\frac{1}{3} + \sum_{n=1}^{\infty} (-1)^{n+1} \frac{(x-5)^n}{3^{n+1}}$