

Problem 2b page 131

x	f(x)
0.1	-0.62049958
0.2	-0.28398668
0.3	0.00660095
0.4	0.2484244
	-3.365129
	2.9058763
	-2.2962635
	2.4182345
	-2.438209
	-0.473151667

linear: $L1(x) = -0.62049958 + 3.365129(x-0.1)$ quadratic: $L2(x) = -0.62049958 + 3.365129(x-0.1) - 2.2962635(x-0.1)(x-0.2)$ cubic: $L3(x) = -0.62049958 + 3.365129(x-0.1) - 2.2962635(x-0.1)(x-0.2)$
 $-0.473151667(x-0.1)(x-0.2)(x-0.3)$ values: $L1(0.25) = -0.11573023$
 $L2(0.25) = -0.13295218$
 $L3(0.25) = -0.132774749$ **Problem 5a page 131**

x	f(x)
0	1
0.2	1.2214
0.4	1.49182
0.6	1.82212
0.8	2.22554
	1.107
	1.3521
	0.61275
	1.6515
	0.7485
	0.22625
	2.0171
	0.914
	0.275833333
	0.061979167

 $L4(0.05) = 1.051258799$

0.05

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x	f(x)	derivative values			
0	0				
0	0	75			
3	225	75	0		
3	225	77	0.666666667	0.222222222	
5	383	79	1	0.066666667	-0.031111111
5	383	80	0.5	-0.25	-0.063333333
8	623	80	0	-0.1	0.03
8	623	74	-2	-0.666666667	-0.113333333
13	993	74	0	0.25	0.114583333
13	993	72	-0.4	-0.08	-0.04125

Continuation:

-0.031111111
 -0.063333333 -0.006444444
 0.03 0.011666667 0.002263889
 -0.113333333 -0.028666667 -0.00504167 -0.000913194
 0.114583333 0.022791667 0.005145833 0.000783654 0.000130527
 -0.04125 -0.019479167 -0.00422708 -0.000937292 -0.00013238

Continuation:

-2.02236E-05

finished in Maple

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> ## Problem 7 page 140
> ## Continuation:
> x0:=0;
x1:=3;
x2:=5;
x3:=8;
x4:=13;
a0:=0;
a1:=75;
a2:=0;
a3:=0.222222222;
a4:=-0.031111111;
a5:=-0.006444444;
a6:=0.002263889;
a7:=-0.000913194;
a8:=0.000130527;
a9:=-0.0000202236;

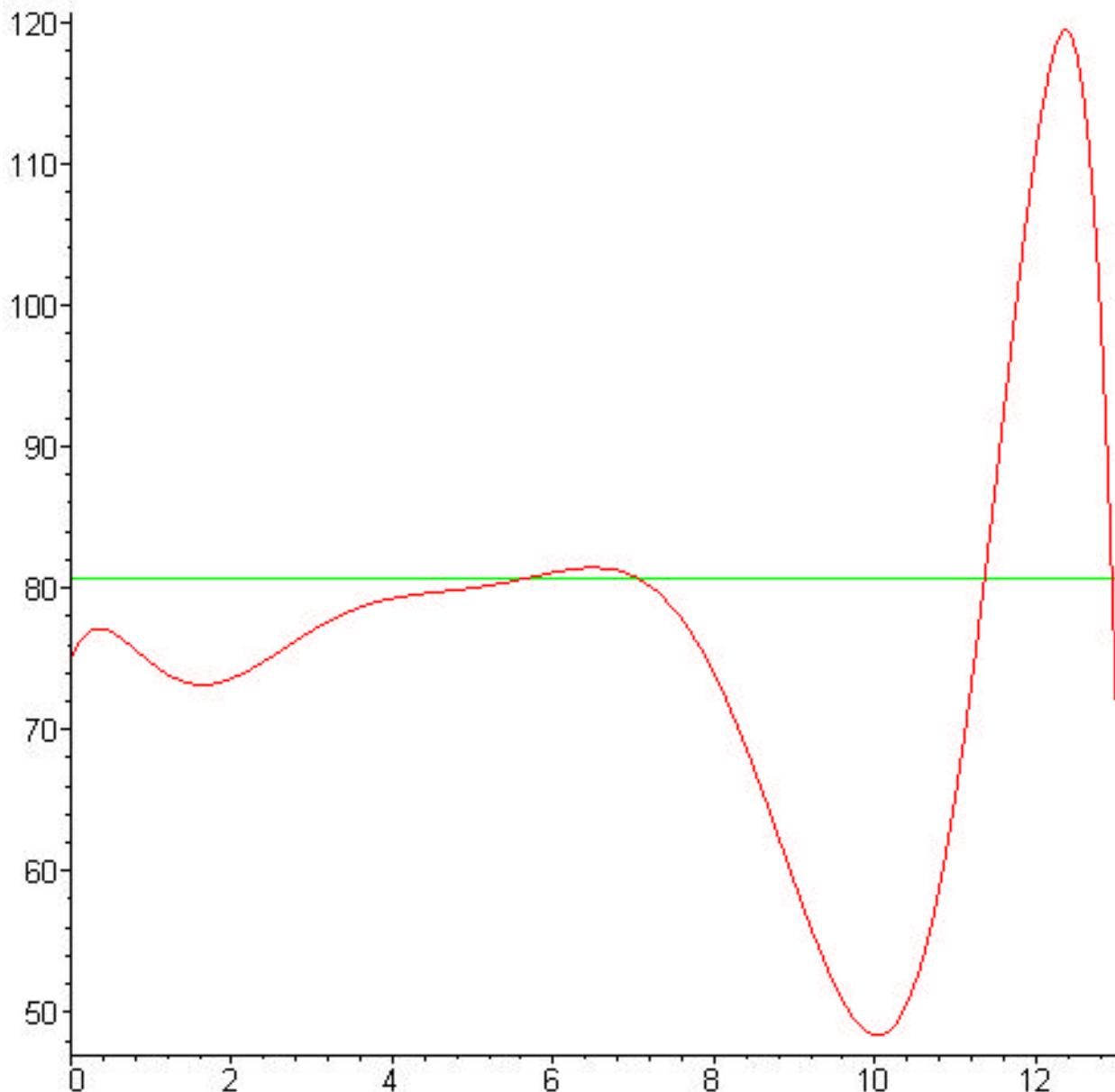
H9:=x->a0+a1*(x-x0)+a2*(x-x0)^2+a3*(x-x0)^2*(x-x1)+a4*(x-x0)^2*(x-x1)^2+a5*(x-x0)^2*(x-x1)^2*(x-x2)+a6*(x-x0)^2*(x-x1)^2*(x-x2)^2+a7*(x-x0)^2*(x-x1)^2*(x-x2)^2*(x-x3)+a8*(x-x0)^2*(x-x1)^2*(x-x2)^2*(x-x3)^2+a9*(x-x0)^2*(x-x1)^2*(x-x2)^2*(x-x3)^2*(x-x4):
simplify(H9(x));

```

$x0 := 0$
 $x1 := 3$
 $x2 := 5$
 $x3 := 8$
 $x4 := 13$
 $a0 := 0$
 $a1 := 75$
 $a2 := 0$
 $a3 := 0.222222222$
 $a4 := -0.031111111$
 $a5 := -0.006444444$
 $a6 := 0.002263889$
 $a7 := -0.000913194$
 $a8 := 0.000130527$

$$a9 := -0.0000202236$$

```
75.  $x - 0.02187564600 x^7 + 7.161904260 x^2 - 10.09530361 x^3 + 5.508117381 x^4$ 
    $- 1.538294606 x^5 + 0.2430410630 x^6 + 0.001040589000 x^8 - 0.00002022360000 x^9$ 
> dH9:=D(H9):
simplify(dH9(x));
evalf(H9(10));
evalf(dH9(10));
75. + 14.32380852 x + 0.008324712000 x^7 - 30.28591082 x^2 + 22.03246952 x^3
   - 7.691473030 x^4 + 1.458246378 x^5 - 0.1531295220 x^6 - 0.0001820124000 x^8
   742.5030280
   48.38202660
>## 55 mi/h = 55* 5280 feet / 3600 sec
evalf(55*5280/3600);
80.66666667
> plot([dH9,80.66666667],0..13);
```



```

>## To find the first time the speed exceeds 55mi/h we solve
## dH9(x)=80.66666667 using Newton's method
## close to time 6 sec
d2H9:=D(dH9):
g:=x->evalf(x-(dH9(x)-80.66666667)/d2H9(x)):
x:=5.9;
for i from 1 to 3 do
x:=g(x);
od;

```

$x := 5.9$

$x := 5.643807884$

$x := 5.648806090$

$x := 5.648802676$

```

> ## Answer: The speed of 55 mi/h is first exceeded at t= 5.6488.
## To find the maximum speed we solve d2H9(x)=0
## using Newton method close to time 12
d3H9:=D(d2H9):
gg:=x->evalf(x-(d2H9(x))/d3H9(x)):
x:=12;
for i from 1 to 5 do
x:=gg(x);
od;
x := 12
x := 12.64532344
x := 12.42890015
x := 12.37498784
x := 12.37187974
x := 12.37186978

> ## Answer: The maximal speed is attained at t=12.3719
## and equals:in feet/sec
evalf(dH9(12.3719));
119.4220060

```

>