McGill University Math 370A: Algebra III Assignment 4: due Friday, October 31 , 1997

- 1. Show that $\operatorname{Aut}(C_2 \times C_4) \cong D_4$.
- 2. Show that the groups $G_i = \langle x, y : x^8, y^2, yxy^{-1}x^{-i} \rangle$ with i=1,3,5,7 are non-isomorphic groups of order 16.
- 3. Text: p. 70, #2
- 4. Text: p. 78, #2.
- 5. Text: p. 78, #4.
- 6. Text: p. 78, #5.
- 7. Text: p. 78, #6.
- 8. Text: p. 82, #2.
- 9. Find, up to isomorphism, all groups of order 18.
- 10. If G is the group of symmetries of a cube, show that $G/C(G) \cong S_4$.