McGill University

Math 240: Discrete Structures 1

Assignment 1: due Friday, September 16, 2005

Reading: Text: 1.1: Logic, 1.2: Propositional Equivalences, 1.3: Predicates and Quantifiers, 1.4: Nested Quantifiers, 1.6: Sets, 1.7: Set Operations

Questions:

1. Using truth tables, show that the following propositions are tautologies.

(a)
$$((p \lor q) \land (\neg p \lor r)) \rightarrow (q \lor r)$$

(b)
$$((p \lor q) \land (p \to r) \land (q \to r)) \to r$$

2. Without using truth tables, prove that the following propositions are logically equivalent.

(a)
$$p \leftrightarrow q$$

(b)
$$(p \land q) \lor (\neg p \land \neg q)$$

(c)
$$\neg (p \oplus q)$$

3. If A, B, C are sets, prove or disprove the following statements:

(a)
$$(A \cup C = B \cup C) \rightarrow (A = B)$$

(b)
$$(A \cap C = B \cap C) \rightarrow (A = B)$$

(c)
$$(A \oplus B) \cap C = (A \cap C) \oplus (B \cap C)$$

(d)
$$(A \oplus B) \cup C = (A \cup C) \oplus (B \cup C)$$

4. If A, B, C are sets, prove that $A \oplus (B \oplus C) = (A \oplus B) \oplus C$.