1. Find if the following series are divergent, conditionally convergent or absolutely convergent. (Justify your answers).

(a)
$$\sum_{n=1}^{\infty} \frac{\sqrt{n+1} - \sqrt{n}}{n^{\frac{3}{4}}}$$
 $(-1)^n$ (b) $\sum_{n=1}^{\infty} \frac{(-1)^n \cdot \sin(\frac{1}{n})}{n^{\frac{1}{4}}}$
(c) $\sum_{n=1}^{\infty} \frac{(n!)^2 \cdot (-1)^n}{e^{n^2}}$

2. If
$$Si(x) = \int_0^x \frac{\sin t}{t} dt$$
,

- (a) find a power series for Si(x) about x = 0,
- (b) for what values of x does the series converge
- (c) find Si(0.3) to 5 decimals. (Show the value of each term used and justify your accuracy.)
- 3. Find the radius of convergence and interval of convergence of the following series:

(a)
$$\sum_{n=2}^{\infty} \frac{(-1)^n (2x-4)^{2n}}{16^n \cdot n^2}$$

(b) $\sum_{n=1}^{\infty} \frac{9^n x^n}{(\ln(n+1))^n}$

4. For $t \ge 0$, the parametric representation of the curve C is

$$x = t$$
, $y = 4t^{\frac{3}{2}}/3$, $z = t^2$.

- (a) Find the unit tangent, unit normal, and curvature at any point.
- (b) Find the arc length of C cut off between z = 0 in z = 4
- (c) If t is time, find the tangential and normal components of acceleration at any point.

5. (a) Find the critical (stationary) points

$$z = xy(4 - x - y)$$

- (b) Classify the points as maximum, minimum or saddle points.
- 6. Sketch the region integration for the following integral

$$\int_{x=0}^{3} \int_{y=0}^{\sqrt{9-x^2}} (x^2 + y^2) \cdot e^{(x^2 + y^2)} dy \cdot dx$$

Now evaluate the integral.

- 7. If a body is bounded by the cone $z = 6 \sqrt{x^2 + y^2}$. and the paraboloid $z = x^2 + y^2$, with the density of the material being $\rho(x, y, z) = \sqrt{x^2 + y^2}$, find the mass of the body.
- 8. (a) Let $w = z^3 + 3z + 2x^2 + 3y^2$. Find ∇w at any point (x, y, z).
 - (b) For the surface $z^3 + 3z + 2x^2 + 3y^2 = 9$, show that (1, 1, 1) lies on the surface and find the tangent plane and normal line to the surface at (1, 1, 1).
 - (c) The equation in (b) defines z = f(x, y) with f(1, 1) = 1. Find

$$f_x(x,y) = \frac{\partial z}{\partial x}, \quad f_y(x,y) = \frac{\partial z}{\partial y}$$

and then find $f_{xx}(1,1)$, $f_{xy}(1,1)$ and $f_{yy}(1,1)$ and expand f(x,y) as a Taylor series about (1,1) as far as the second degree terms.