# 556: MATHEMATICAL STATISTICS I

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Office Hours: Monday 16:00-17:50

Thursday 12:00-13:30

Other appointments available if needed.

Textbook: Statistical Inference (2nd Ed)

by G. Casella and R. L. Berger.

#### TARGET SYLLABUS

- 1 Preliminaries
  - 1.1 Probability
  - 1.2 Random Variables
- 2 Univariate and Multivariate Distributions
- 3 Transformations and Expectations
  - 3.1 Transformations
  - 3.2 Expectations
- 4 Families of distributions
  - 4.1 Location-Scale Families
  - 4.2 Exponential Families
  - 4.3 Convolution Families and Exponential Dispersion Models
  - 4.4 Hierarchical Models
- 5 Some Inequalities
  - 5.1 Concentration inequalities
    - 5.1.1 Markov's inequality
    - 5.1.2 Chebyshev's inequality
    - 5.1.3 Chernoff bounds
  - 5.2 Cauchy-Schwarz Inequality
  - 5.3 Jensen's Inequality
- 6 Sampling Distributions
  - 6.1 Definitions
  - 6.2 Sampling from Families
    - 6.2.1 Sampling from a Location-Scale Family
    - 6.2.2 Sampling from an Exponential Family
    - 6.2.3 Sampling from a Normal Family
- 7 Convergence concepts
  - 7.1 Convergence in Probability: The Weak Law of Large Numbers
  - 7.2 Convergence Almost Surely: The Strong Law of Large Numbers
  - 7.3 Weak Convergence
  - 7.4 A Central Limit Theorem
- 8 The Delta Method
- 9 Random Number Generation

# **EVALUATION: DETAILS**

Please note that the method of evaluation for this class will be on the following basis only $^{\ddagger}$ :

Coursework Assignments Bi-Weekly

Beginning Thursday 11th September 2008 Hand-in 18th September, 5pm deadline

Mid-Term 1.5 hours

Tuesday 21st October 2008

In class Closed book

Final 3 hours

4th-19th December 2008 (exact date to be confirmed)

Venue to be confirmed

Closed book

Final mark for course<sup>‡</sup>: the larger of

20 % Coursework + 20 % Mid-Term + 60 % Final

and

20 % Coursework + 80 % Final

### **NOTES**:

‡ There will no opportunity for a make-up Mid-Term if this examination is missed, and no make-up work in place of any aspect of the course assessment.

#### **ACADEMIC INTEGRITY**

McGill University values academic integrity. Therefore all students must understand the meaning and consequences of cheating, plagiarism and other academic offences under the Code of Student Conduct and Disciplinary Procedures (see

http://www.mcgill.ca/integrity/

for more information).

David A. Stephens. September 2, 2008