quiz 2 math228, classical geometry fall 2021

The quiz is worth 10 points. Justify all your claims rigourously.

- a. State Ceva's theorem. (3 points)
- **b.** Let *ABC* be a triangle and let *X* be a point on *ABC* different than *A* such that *X* bisects the perimeter of *ABC*. For example, in the following drawing, |AC| + |CX| = |AB| + |BX|.



Argue that X will always lie on the segment BC. Thus, the segment AX is a cevian, called a *splitter* of ABC. (bonus 5 points)

c. Show that the three splitters (defined in b.) of a triangle are concurrent.



Their common intersection if called the Nagel point of ABC. (7 points)