Hour 04

1. Does the series  $1 + 1 + 1 + \cdots$  converge or diverge? If it converges, what is its sum?

2. Does the series  $1 + (-1) + 1 + (-1) + \cdots$  converge or diverge? If it converges, what is its sum?

3. (a) Does the series  $1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \cdots$  converge or diverge? If it converges, what is its sum?

(b) Draw a diagram showing the first 6 partial sums of the series  $1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \cdots$ .

- 4. In this problem, you'll investigate the series  $\sum_{k=1}^{\infty} \frac{2}{(2k)^2 1}$ .
  - (a) Write out the first 4 terms of the series.

(b) Find the first 4 partial sums of the series. Express them as simplified fractions.

(c) Looking at your answer to 4b, guess a formula for the *n*-th partial sum.

(d) Based on your guess from part (c), does the series converge or diverge? If it converges, what is its sum?

5. (a) Draw a partial sum diagram showing the first 6 partial sums of the series  $\sum_{k=0}^{\infty} \left(-\frac{1}{2}\right)^k$ .

(b) Based on your diagram, do you think the series  $\sum_{k=0}^{\infty} \left(-\frac{1}{2}\right)^k$  converges or diverges?

6. Here is a diagram showing the first 6 partial sums of an unknown series  $\sum_{k=1}^{\infty} a_k$ .



(a) From the diagram, determine whether each of  $a_1, a_2, \ldots, a_6$  is positive, negative, or zero.

(b) Which of  $a_1, a_2, \ldots, a_6$  is biggest in magnitude?