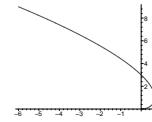


1. (a)  $x = t - \frac{1}{3}t^3$ ,  $y = t^2$

(b) VT: at  $(\frac{2}{3}, 1)$  ( $t = 1$ ) HT: at  $(0, 0)$  ( $t = 0$ )

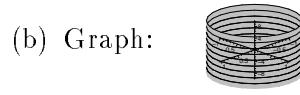
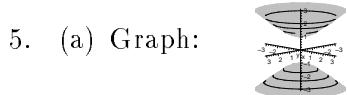
(c)  $s = 12$



2.  $\sqrt{9.1} = 3 + \frac{1}{6}(0.1) \pm \frac{1}{216}(0.1)^2 = 3.016667 \pm 0.000046$

3.  $1 + \frac{1}{2!}x^2 + \frac{1}{4!}x^4 + \frac{1}{6!}x^6 + \cdots + \frac{1}{(2n)!}x^{2n} + \cdots$

4.  $\frac{1}{3}x^3 + \frac{1}{7}x^7 + \frac{1}{11}x^{11} + \cdots + \frac{1}{4n-1}x^{4n-1} + \cdots$  Interval of convergence:  $(-1, 1)$



6.  $T = \frac{1}{1+2t^2}\langle 2t, 1, 2t^2 \rangle$ ,  $N = \frac{1}{1+2t^2}\langle 1 - 2t^2, -2t, 2t \rangle$ ,  $\kappa = \frac{2t}{(1+2t^2)^2}$ ,  $a_T = \frac{2t^2-1}{t^2}$ ,  $a_N = \frac{2}{t}$

7. The limit  $\lim_{(x,y) \rightarrow (0,0)} \frac{\sin(x^2 + y^2)}{x^2 + y^2} = 1 = f(0,0)$  so the function is continuous.

8. (a)  $-\frac{6}{5\sqrt{2}}$  (b)  $\nabla f = \left\langle \frac{2}{5}, -\frac{4}{5} \right\rangle$ ;  $|\nabla f| = \frac{2}{\sqrt{5}}$  (c)  $\mathbf{u} = \left\langle \frac{2}{\sqrt{5}}, \frac{1}{\sqrt{5}} \right\rangle$  or  $\left\langle \frac{2}{\sqrt{5}}, -\frac{1}{\sqrt{5}} \right\rangle$

9. (a)  $-x + y - 6z = 8$  (b)  $f(0.1, 1.9) \simeq -1.03333$

10.  $\frac{\partial z}{\partial x} = 2xyf'$ ,  $\frac{\partial z}{\partial y} = f - 2y^2f'$  (so qed)

11. CPs:  $(-1, \pm 2)$  are saddle points,  $(-\sqrt{5}, 0)$  is a local max,  $(\sqrt{5}, 0)$  is a local min.12. max  $(4\sqrt{3})$  at  $(2\sqrt{3}, -\sqrt{3}, \sqrt{3})$ ; min  $(-4\sqrt{3})$  at  $(-2\sqrt{3}, \sqrt{3}, -\sqrt{3})$ 

13. (a)  $\mathbf{b}, \mathbf{c}$  (b)  $\pi$  (the region is a circle...)

14.  $\frac{2}{3}(e-1)$  15.  $99\pi$

16.  $V = \int_0^{2\pi} \int_{\pi/4}^{\pi/2} \int_0^{\csc \phi} d\rho d\phi d\theta = \int_0^{2\pi} \int_0^1 \int_0^r r dz dr d\theta = \frac{2}{3}\pi$

