



## Cal II (S) (Maths 201–NYB)

## Answers

1. The integrals:

$$(a) \frac{2}{15}(x^3 - 1)^{5/2} + \frac{2}{9}(x^3 - 1)^{3/2} + C \quad \text{or} \quad \frac{2}{9}x^3(x^3 - 1)^{3/2} - \frac{4}{45}(x^3 - 1)^{5/2} + C$$

$$(b) \frac{2}{9}(x^3 - 1)^{3/2} + C$$

$$(c) \frac{1}{2} \ln |2t + \sqrt{4t^2 - 9}| + C$$

$$(d) \frac{\sqrt{3}}{16} - \frac{\pi}{48}$$

$$(e) -2(\sec t)^{-1/2} + C$$

$$(f) \frac{1}{25} \tan^5 5\theta + \frac{1}{35} \tan^7 5\theta + C$$

$$(g) \frac{1}{2} \left( \left( \frac{\pi}{3} \right)^4 - \left( \frac{\pi}{4} \right)^4 \right) = \frac{175\pi^4}{41472}$$

$$(h) 2e^{1+\sqrt{x}} + C$$

$$(i) \frac{1}{2}t + \frac{1}{4} \sin 2t - \frac{1}{3} \sin^3 2t + \frac{1}{10} \sin^5 2t + C$$

$$(j) -\frac{\sqrt{1-x^2}}{x} - \arcsin(x) + C$$

$$(k) \frac{1}{10} e^x \sin 3x - \frac{3}{10} e^x \cos 3x + C$$

$$(l) \frac{1}{4}x^3 e^{4x} - \frac{3}{16}x^2 e^{4x} + \frac{3}{32}x e^{4x} - \frac{3}{128} e^{4x} + C$$

2.  $\frac{\pi}{6} + \frac{1}{2\sqrt{3}}$

3. The derivative is:  $-\frac{1}{2+2x+x^2}$

4. Simplified: (a)  $5/13$  (b)  $\frac{\pi}{4}$  (c)  $\frac{1}{x}$

(d)  $\tan \theta = \pm\sqrt{8}$  but  $\tan \left( \arccos \left( -\frac{1}{3} \right) \right) = -\sqrt{8}$ . In the former case,  $\theta$  could be in QII or QIII, but in the latter case, it must be in QII, where  $\tan$  is negative.

5. (a) Any  $x$  (strictly) between  $-\frac{\pi}{2}$  and  $\frac{\pi}{2}$  will satisfy  $\arctan(\tan x) = x$ ; no  $x$  outside that range will, since the **range** of  $\arctan x$  is  $(-\frac{\pi}{2}, \frac{\pi}{2})$ .

(b) Any  $x$  will satisfy  $\tan(\arctan x) = x$ , since the **domain** of  $\arctan x$  is  $(-\infty, \infty)$ .