



1. Evaluate these integrals:

$$\begin{array}{lll}
 \text{(a)} \int \frac{\cos^5 x \, dx}{\sin^4 x} & \text{(b)} \int \frac{x^2 + x - 1}{(x+1)(x^2-1)} \, dx & \text{(c)} \int \frac{\csc^4 x \, dx}{\sqrt[3]{\cot x}} \\
 \text{(d)} \int \sin^2\left(\frac{x}{4}\right) \cos^2\left(\frac{x}{4}\right) \, dx & \text{(e)} \int \frac{x^2 - 2x}{x^3 - 3x^2} \, dx & \text{(f)} \int \frac{dx}{(x^2 + 9)^2} \\
 \text{(g)} \int \frac{dx}{x^4 - 1} & \text{(h)} \int \sec^4 x \tan^3 x \, dx & \text{(i)} \int \frac{dx}{\sqrt{1-x^2} \arcsin(x)} \\
 \text{(j)} \int \frac{4x^3 - 6x^2 - 1}{2x^2 - 5x - 3} \, dx & \text{(k)} \int x^2 e^{2x} \, dx & \text{(l)} \int \frac{x^3 + x^2 + x - 1}{x^4 + x^2} \, dx \\
 \text{(m)} \int_{\frac{1}{\sqrt{2}}}^1 \arcsin x \, dx & \text{(n)} \int \cos(\ln x) \, dx & \text{(o)} \int_1^{\sqrt{3}} \frac{\sqrt{x^2 + 1}}{x^4} \, dx
 \end{array}$$

2. Evaluate:

$$\begin{array}{lll}
 \text{(a)} \int_0^{\frac{\pi}{2}} \frac{dx}{\sin x} & \text{(b)} \int_0^3 \frac{dx}{\sqrt[3]{x-1}} & \text{(c)} \int_1^{\infty} \frac{e^{-\sqrt{x}}}{\sqrt{x}} \, dx \\
 \text{(d)} \int_0^4 \frac{x \, dx}{x-2} & \text{(e)} \int_2^{\infty} \frac{dx}{x^2-1} &
 \end{array}$$

3. Evaluate:

$$\begin{array}{lll}
 \text{(a)} \lim_{x \rightarrow 0} \frac{\arctan x}{\tan 2x} & \text{(b)} \lim_{x \rightarrow 0^+} x \ln(x^2) & \text{(c)} \lim_{x \rightarrow 1^+} \left(\frac{1}{\ln x} + \frac{1}{1-x} \right) \\
 \text{(d)} \lim_{x \rightarrow 0^+} x^{1/(\ln(e^x - 1))} & \text{(e)} \lim_{x \rightarrow 0} (1 + \sin 3x)^{(1/x)} & \text{(f)} \lim_{x \rightarrow 0^+} (\cos x)^{(1/x^2)}
 \end{array}$$

4. Find the area between:

$$\text{(a)} y = x^3 - 2x \text{ and } y = 3x; \quad \text{(b)} x - 3y = 0 \text{ and } x + y = y^3 \text{ above the } x \text{ axis;}$$

5. Find the volume of the solid obtained when the region between the curves $y = 2x - x^2$ and $y = x^3$ above the x -axis is rotated (a) about the y -axis; (b) about the x -axis.6. Find the volume of the solid obtained when the region between $y = \sin x$, $y = 0$, $x = 0$, and $x = \pi$ is rotated about the line $x = 5$.7. Solve the following differential equations; write your answer as explicit functions $y = f(x)$ (with a suitable constant c).

$$\begin{array}{lll}
 \text{(a)} \frac{dy}{dx} = \frac{y}{x^2 - 1} & \text{(b)} y' = y(1 - y) & \text{(c)} \frac{dy}{dx} = \frac{x \sec y}{1 + x^2}
 \end{array}$$

8. Solve the following initial value problems.

$$\text{(a)} y' = xy^2; y(0) = 1 \quad \text{(b)} y' = e^{-y} \sqrt{x}; y(1) = 0$$

9. Find the arclength of the following curves on the given intervals:

$$\text{(a)} y = \frac{1}{6}x^5 + \frac{1}{10}x^{-3} \text{ on } [1, 2] \quad \text{(b)} y = \frac{1}{3}x^{3/2} - \sqrt{x} \text{ on } [1, 4]$$