Name:
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1. Evaluate the following integral:

$$
\int \frac{x^{2}+x-1}{(x+1)\left(x^{2}-1\right)} d x
$$

2. Evaluate the limit $\lim _{x \rightarrow 0}(1+\sin 3 x)^{(1 / x)}$
3. Find the arclength of the curve $y=\frac{1}{2} x^{2}-\frac{1}{4} \ln (x)$ from $x=2$ to $x=4$.
4. Solve the differential equation, giving your answer as an explicit function $y=f(x)$ :

$$
3 \mathrm{e}^{x} y^{2} y^{\prime}=x, \quad y(0)=0
$$

5. Find the volume of the solid obtained when the region above the $x$-axis, between the curves $y=2 x-x^{2}$ and $y=x^{3}$, is rotated about the $y$-axis.


## Answers

1. $\frac{3}{4} \ln |x+1|-\frac{1}{2(x+1)}+\frac{1}{4} \ln |x-1|+C$
2. $\mathrm{e}^{3}$
3. $6+\frac{1}{4} \ln 2$
4. $y=\sqrt[3]{1-x \mathrm{e}^{-x}-\mathrm{e}^{-x}}$
5. $\frac{13 \pi}{30}$
