McGill University Math 325B: Differential Equations Assignment 2B: due Thursday, January 24, 2000

1. Find the solution of the initial value problem

$$yy' = xy^3$$
, $y(0) = b > 0$.

What is its interval of definition? (Your answer will depend on the value of b.) Sketch the graph of the solution when $b=\pm\frac{1}{2},\,\pm 1,\,\pm 2$

2. Find the general solution of the differential equation

$$\frac{dy}{dx} + y^3x + y = 0.$$

What is the solution satisfying y(0) = 1.

3. Find the general solution of the differential equation

$$2xy\frac{dy}{dx} = x^2 + y^2.$$

Sketch the integral curves.

4. Solve the initial value problem

$$2xy\frac{dy}{dx} = (x-1)e^x + y^2, \quad y(1) = 1.$$