

We will show that the the optimal transport problem

$$\inf_{\pi} \int c(x - y) \pi(dx dy), \quad \pi \in \Pi(\mu, \nu)$$

with $c : \mathbb{R}^d \rightarrow \mathbb{R}^d$ convex has a solution of the form $\pi = (\text{Id}, T)_{\#} \mu$. The proof is based on a decomposition of Sudakov's type.