McGill University Department of Mathematics and Statistics

MATH 316 (Complex Variables) COURSE OUTLINE – Fall Semester 2007

Instructor: Dr. Pengfei Guan (Burnside Hall 918),

telephone: 398-3806, Email: guan@math.mcgill.ca Office hours: Tuesday & Thursday, 10am-11:30am, or by appointment. Course Webpage: http://www.math.mcgill.ca/guan/courses/m316.html

Textbook: Complex Variables with Applications by A.D. Wunsch, 3rd ed. (Addison-Wesley)

References:

- (1) Complex Variables and Applications (6th Ed, McGraw-Hill), by Brown and Churchill.
- (2) Complex Variables by M.R. Spiegel (Schaum's McGraw-Hill).

Course Outline:

- (1) Analytic functions of one complex variable: limits, continuity, differentiation, analytic functions, Cauchy-Riemann equation, harmonic functions.
- (2) *Elementary functions:* basic properties of the exponential, trigonometric, hyperbolic, logarithmic and inverse functions, concept of branches.
- (3) *Complex integration:* Integrals of complex-valued functions, contour integrals, Cauchy Theorem, Cauchy's Integral Formulas, the Argument Principle, Rouche's Theorem and applications.
- (4) *Infinity Series:* convergence of power series, Taylor's series, Laurent expansion, singularities, residues, the Residue Theorem, Cauchy principal value integrals and Fourier transforms integrals.
- (5) Complex inversion integrals for Laplace Transforms: applications to heat and wave equations.
- (6) Conformal Mappings: maximum modulus theorem, properties of conformal mappings, Schwarz-Christoffel transformation, Dirichlet and Neumann problems for Laplace's equation, complex potential and applications.

Assignments: There will be six assignments, due on following Thursdays by 5:00pm: Sept. 20, Oct. 4, 18, Nov. 1, 15, 29. NO LATE ASSIGNMENTS WILL BE ACCEPTED.

Middle Term Tests: to be scheduled.

Final Examination: to be scheduled.

Marking System: Assignments 15%; Tests 35%; and Final Examination 50%.

The Senate of the University has resolved that the following statement be included in this course outline: "McGILL UNIVERSITY VALUES ACADEMIC INTEGRITY. THEREFORE ALL STUDENTS MUST UNDERSTAND THE MEANING AND CONSEQUENCES OF CHEATING, PLAGIARISM AND OTHER ACADEMIC OFFENSES UNDER THE CODE OF STUDENT CONDUCT AND DIS-CIPLINARY PROCEDURES (see www.mcgill.ca/integrity for more information)."