

Note: Here

	DOSE 0	DOSE 1	DOSE 2	DOSE 3
s_i^2	8.018	5.873	11.315	3.875

so we might suspect that the treatment variances $\sigma_1^2, \sigma_2^2, \sigma_3^2, \sigma_4^2$ are not equal. We may test this formally using

LEVENE'S TEST

- SPSS can report this test result.

Note: Visual inspection can give an idea of whether the equal variance assumption is valid, or whether the populations are normal. **But the sample sizes may be small, so that visual inspection or testing may not detect deviations from these assumptions.**

Ideally we would like to be able to relax these assumptions.

The ANOVA Table

For a completely randomized design, we may report the results of the ANOVA F-test in a stylized form, the **ANOVA Table**

SOURCE	DF	SS	MS	F
TREATMENTS	$k - 1$	SST	$MST = \frac{SST}{(k - 1)}$	$F = \frac{MST}{MSE}$
ERROR	$n - k$	SSE	$MSE = \frac{SSE}{(n - k)}$	
TOTAL	$n - 1$	SS		

Note

(i) $(k - 1) + (n - k) = (n - 1)$

(ii) $SST + SSE = SS$

i.e. we can fill in missing values if they are not given.

Sometimes an extra column is added at the right of the table to give the p -value of the ANOVA F-test.

SOURCE	DF	SS	MS	F	p
TMT	$k - 1$	SST	MST	$F = \frac{MST}{MSE}$	p -val
ERROR	$n - k$	SSE	MSE		
TOTAL	$n - 1$	SS			

where p -val solves

$$\frac{MST}{MSE} = F_{p\text{-val}}(k - 1, n - k)$$

and $F_{\alpha}(\nu_1, \nu_2)$ is the $(1 - \alpha)$ probability point of the Fisher-F distribution.

SPSS Handout: Examples

- ▶ **DIET**: milk-protein level example (p. 1)
- ▶ **DOSE-LEVEL**: pull-strength in Alzheimer's example (p. 3)
- ▶ **DIAGNOSIS**: (p. 5)
 - ▶ **RESPONSE**: gut permeability of drug mannitol in AIDS/HIV patients
 - ▶ **FACTOR**: AIDS/HIV Status
 - ▶ **FACTOR LEVELS**: $k = 4$
 - ▶ AIDS - Full AIDS
 - ▶ ARC - AIDS-related conditions
 - ▶ HIV+ - HIV positive
 - ▶ HIV- - HIV negative

SPSS Handout: Examples

- ▶ **BATCH NUMBER:** bacteria level (per mill.) in different batches of milk (p. 7)
 - ▶ RESPONSE: Bacteria level count per million
 - ▶ FACTOR: Batch number
 - ▶ FACTOR LEVELS: 1,2,3,4,5 ($k = 5$)
- ▶ **TREATMENT GROUP:** Post-traumatic stress disorder (PTSD) score in different treatment groups(p. 9)
 - ▶ RESPONSE: PTSD score
 - ▶ FACTOR: Therapeutic treatment method
 - ▶ FACTOR LEVELS: $k = 4$
 - ▶ SIT - "Stress Inoculation Therapy"
 - ▶ RE - "Relive Experience"
 - ▶ SC - "Standard Counselling"
 - ▶ WL - "Waiting List" (Control)