## MATH 204 - SOLUTIONS 5

For these questions we will use the method of ANOVA-F testing for nested models, and the test statistic

$$
F=\frac{\left(S S E_{R}-S S E_{C}\right) /(k-g)}{S S E_{C} /(n-k-1)}
$$

where $S S E_{R}$ is the error sum of squares for the Reduced Model, specified using $g+1$ parameters including the intercept, and $S S E_{C}$ is the error sum of squares for the Complete Model, specified using $k+1$ parameters including the intercept.
If the reduced model is an adequate simplification of the complete model, then

$$
F \sim \text { Fisher-F }(k-g, n-k-1)
$$

Note here that

$$
k-g=(n-g-1)-(n-k-1)=\mathrm{EDF}_{R}-\mathrm{EDF}_{C}
$$

so the $k-g$ quantities can be deduced directly from the EDFs.
The SPSS output is attached.

1. Oysters Data Set Here we can fit the five models listed below. For these data $n=20$.

|  | Model | $k$ | EDF | SSE |
| :--- | :--- | :---: | :---: | ---: |
| M0 | Null | 0 | 19 | 358.670 |
| M1 | trt | 4 | 15 | 160.263 |
| M2 | initialwt | 1 | 18 | 16.312 |
| M3 | trt + initialwt | 5 | 14 | 4.222 |
| M4 | trt + initialwt + trt. initialwt | 9 | 10 | 2.834 |

Inspection of the ANOVA tables implies that, rather than go through forward or backward selection, we might start with the model M3, trt + initialwt, and try to include or omit terms.

- M3 vs M4

$$
F=\frac{(4.222-2.834) /(9-5)}{2.834 / 10}=1.224
$$

From tables Fisher- $\mathrm{F}_{0.05}(4,10)=3.48>1.224$, so we do not reject M 3 as an adequate simplification of M4.

- M1 vs M3

$$
F=\frac{(160.263-4.222) /(5-4)}{4.222 / 14}=517.462
$$

From tables Fisher- $\mathrm{F}_{0.05}(1,14)=4.60<517.462$, so we reject M 1 as an adequate simplification of M3.

- M2 vs M3

$$
F=\frac{(16.312-4.222) /(5-1)}{4.222 / 14}=10.022
$$

From tables Fisher- $\mathrm{F}_{0.05}(4,14)=3.11<10.022$, so we reject M 2 as an adequate simplification of M3.
Hence the most suitable model is M3. The $R^{2}$ and Adjusted $R^{2}$ values are 0.988 and 0.984 , indicating that the fit is very good.
2. Oranges Data Set Here we have two regression models for Q1 and Q2 in terms of the predictors. For these data $n=36$.

First for Q1 ; note that we cannot fit the interaction day . store as we do not have sufficient data, as we only have one replicate per day $\times$ store combination.
The models are listed in the order they are presented in the output:

|  | Model | $k$ | EDF | SSE |
| :--- | :--- | :---: | :---: | ---: |
| M0 | Null | 0 | 35 | 1622.676 |
| M1 | day + store + P1 + day . P1 + store . P1 | 21 | 14 | 286.786 |
| M2 | day + store + P1 + day . P1 | 16 | 19 | 368.863 |
| M3 | day + store + P1 | 11 | 24 | 447.850 |
| M4 | day + P1 | 6 | 29 | 686.545 |
| M5 | day + P1 + day . P1 | 11 | 24 | 522.153 |
| M6 | P1 | 1 | 34 | 1117.084 |

We proceed with the relevant comparisons:

- M2 vs M1

$$
F=\frac{(368.863-286.786) /(21-16)}{286.786 / 14}=0.801
$$

From tables Fisher- $\mathrm{F}_{0.05}(5,14)=2.96>0.801$, so we do not reject M 2 as an adequate simplification of M1.

- M3 vs M2

$$
F=\frac{(447.850-368.863) /(16-11)}{368.863 / 19}=0.814
$$

From tables Fisher- $\mathrm{F}_{0.05}(5,19)=2.740>0.814$, so we do not reject M 3 as an adequate simplification of M2.

- M4 vs M3

$$
F=\frac{(686.545-447.850) /(11-6)}{447.850 / 24}=2.558
$$

From tables Fisher- $\mathrm{F}_{0.05}(5,24)=2.62>2.558$, so we do not reject M 4 as an adequate simplification of M3, although the result is almost significant.

- M4 vs M5

$$
F=\frac{(686.545-522.153) /(11-6)}{522.153 / 24}=1.511
$$

From tables Fisher- $\mathrm{F}_{0.05}(5,24)=2.62>1.511$, so we do not reject M 4 as an adequate simplification of M5.

- M6 vs M4

$$
F=\frac{(1117.084-686.545) /(6-1)}{686.54 / 29}=3.63
$$

From tables Fisher- $\mathrm{F}_{0.05}(5,29)=2.55<3.63$, so we reject M 6 as an adequate simplification of M4.

Hence it seems that the model day + P1 is the most appropriate model. For this model, the $R^{2}$ and Adjusted $R^{2}$ values are 0.580 and 0.493 respectively, so the explanatory power of the model is only moderate.

Secondly for Q2. The models are listed in the order they are presented in the output:

|  | Model | $k$ | EDF | SSE |
| :--- | :--- | :---: | :---: | ---: |
| M0 | Null | 0 | 35 | 2750.208 |
| M1 | day + store + P2 + day . P2 + store . P2 | 21 | 14 | 275.701 |
| M2 | day + store + P2 + day . P2 | 16 | 19 | 464.396 |
| M3 | day + store + P2 | 11 | 24 | 790.864 |
| M4 | day + P2 | 6 | 29 | 1100.743 |
| M5 | day + P2 + day . P2 | 11 | 24 | 845.661 |
| M6 | P2 | 1 | 34 | 1864.648 |

We proceed with the relevant comparisons

- M2 vs M1

$$
F=\frac{(464.396-275.701) /(21-16)}{275.701 / 14}=1.916
$$

From tables Fisher- $\mathrm{F}_{0.05}(5,14)=2.96>1.916$, so we do not reject M 2 as an adequate simplification of M1.

- M3 vs M2

$$
F=\frac{(790.864-464.396) /(16-11)}{464.396 / 19}=2.671
$$

From tables Fisher- $\mathrm{F}_{0.05}(5,19)=2.740>2.671$, so we do not reject M3 as an adequate simplification of M2, although the result is almost significant.

- M4 vs M3

$$
F=\frac{(1100.743-790.864) /(11-6)}{790.864 / 24}=1.881
$$

From tables Fisher- $\mathrm{F}_{0.05}(5,24)=2.62>1.881$, so we do not reject M 4 as an adequate simplification of M3.

- M4 vs M5

$$
F=\frac{(1100.743-845.661) /(11-6)}{845.661 / 24}=1.448
$$

From tables Fisher- $\mathrm{F}_{0.05}(5,24)=2.62>1.448$, so we do not reject M 4 as an adequate simplification of M5.

- M6 vs M4

$$
F=\frac{(1864.648-1100.743) /(6-1)}{1100.743 / 29}=4.025
$$

From tables Fisher- $\mathrm{F}_{0.05}(5,29)=2.55<4.025$, so we reject M 6 as an adequate simplification of M4.

Hence it seems that the model day + P2 is the most appropriate model. For this model, the $R^{2}$ and Adjusted $R^{2}$ values are 0.600 and 0.517 respectively, so the explanatory power of the model is only moderate.

Note that for the two models, the estimates of the random error variance $\sigma^{2}$ are given by the quantity $S S E / E D F$, so

$$
\text { Q1: } \widehat{\sigma}^{2}=\frac{686.545}{29}=23.674 \quad \text { Q2 }: \widehat{\sigma}^{2}=\frac{1100.743}{29}=37.957
$$

that is, the random error variances seem very different in the two data sets. Hence a combined analysis is not carried out, as this would require a common $\sigma^{2}$.
3. Cotton Data Set For these data $n=49$. Inspection of the SPSS output suggests that we may simplify the full model

$$
\text { variety } \star \text { spacing } \star \text { bollwt }
$$

by dropping some of the higher order interactions. The models compared are listed below:

|  | Model | $k$ | EDF | SSE |
| :--- | :--- | :---: | :---: | ---: |
| M0 | Null | 0 | 48 | 33.091 |
| M1 | variety $\star$ spacing $\star$ bollwt | 7 | 41 | 1.730 |
| M2 | variety + spacing + bollwt + variety . bollwt | 4 | 44 | 1.809 |
| M3 | variety + spacing + bollwt | 3 | 45 | 2.291 |
| M4 | variety + bollwt + variety . bollwt | 3 | 45 | 2.184 |

- M2 vs M1

$$
F=\frac{(1.809-1.730) /(7-4)}{1.730 / 41}=0.624
$$

From tables Fisher- $\mathrm{F}_{0.05}(3,41) \bumpeq 2.84>0.624$, so we do not reject M 2 as an adequate simplification of M1.

- M3 vs M2

$$
F=\frac{(2.291-1.809) /(4-3)}{1.809 / 44}=11.724
$$

From tables Fisher- $\mathrm{F}_{0.05}(1,44)<$ Fisher- $_{0.05}(1,40)=4.08<11.724$, so we reject M3 as an adequate simplification of M2.

- M4 vs M2

$$
F=\frac{(2.184-1.809) /(4-2)}{1.809 / 44}=4.561
$$

From tables Fisher- $\mathrm{F}_{0.05}(2,44)<$ Fisher- $\mathrm{F}_{0.05}(2,40)=3.23$, so we reject M4 as an adequate simplification of M2.

Hence the selected model is M2
variety + spacing + bollwt + variety.bollwt

Parameter estimates confirm that the response is an increasing function of bollwt (coefficient 0.240 , standard error 0.025 ). The $R^{2}$ and adjusted $R^{2}$ of the model are large ( 0.945 and 0.940 ), so the predictive power is high. The residual plot indicates that the final model is adequate.
4. Doses Data Set For these data $n=24$, and we have a balanced complete factorial design. We cannot fit a three-way interaction model as we do not have sufficient replicates (one observation in each combination of the $4 \times 2 \times 3=24$ factor levels). Inspection of the SPSS output suggests that we may simplify the most complex model
bloc + type + dose + bloc.type + bloc.dose + type.dose
by dropping some of the interaction terms. The models compared are listed below:

|  | Model | $k$ | EDF | SSE |
| :--- | :--- | :---: | :---: | ---: |
| M0 | Null | 0 | 24 | 1068.958 |
| M1 | bloc+ type+ dose+ bloc. type+ bloc. dose+ type. dose | 17 | 6 | 74.917 |
| M2 | bloc+ type+ dose+ bloc. dose+ type. dose | 14 | 9 | 122.375 |
| M3 | bloc+ type+ dose+ type. dose | 8 | 15 | 252.458 |
| M4 | bloc+ type+ dose | 6 | 17 | 396.542 |

- M2 vs M1

$$
F=\frac{(122.375-74.917) /(9-6)}{74.917 / 6}=1.267
$$

From tables Fisher- $\mathrm{F}_{0.05}(3,6)=4.76>1.267$, so we do not reject M 2 as an adequate simplification of M1.

- M3 vs M2

$$
F=\frac{(252.458-122.375) /(15-9)}{122.375 / 9}=1.594
$$

From tables Fisher- $\mathrm{F}_{0.05}(6,9)=3.37>1.594$, so we do not reject M 3 as an adequate simplification of M2.

- M4 vs M3

$$
F=\frac{(396.542-252.458) /(8-6)}{252.458 / 15}=4.280
$$

From tables Fisher- $\mathrm{F}_{0.05}(2,15)=3.68<4.28$, so we reject M 4 as an adequate simplification of M3.

No further terms can be dropped from the model, so we select M3
bloc + type + dose + type.dose
as the most suitable model. The $R^{2}$ and adjusted $R^{2}$ of the model are large ( 0.764 and 0.638 ), so the predictive power is good. The residual plot indicates that the final model is adequate.

## Q1. Oysters Data

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $198.407(a)$ | 4 | 49.602 | 4.643 | .012 |
| Intercept | 19028.281 | 1 | 19028.281 | 1780.979 | .000 |
| trt | 198.407 | 4 | 49.602 | 4.643 | .012 |
| Error | 160.263 | 15 | 10.684 |  |  |
| Total | 19386.950 | 20 |  |  |  |
| Corrected Total | 358.670 | 19 |  |  |  |

a R Squared $=.553$ (Adjusted R Squared $=.434$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $342.358(a)$ | 1 | 342.358 | 377.793 | .000 |
| Intercept | 6.466 | 1 | 6.466 | 7.135 | .016 |
| initialwt | 342.358 | 1 | 342.358 | 377.793 | .000 |
| Error | 16.312 | 18 | .906 |  |  |
| Total | 19386.950 | 20 |  |  |  |
| Corrected Total | 358.670 | 19 |  |  |  |

a R Squared = . 955 (Adjusted R Squared $=.952$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $354.447(a)$ | 5 | 70.889 | 235.049 | .000 |
| Intercept | 1.718 | 1 | 1.718 | 5.696 | .032 |
| trt | 12.089 | 4 | 3.022 | 10.021 | .000 |
| initialwt | 156.040 | 1 | 156.040 | 517.384 | .000 |
| Error | 4.222 | 14 | .302 |  |  |
| Total | 19386.950 | 20 |  |  |  |
| Corrected Total | 358.670 | 19 |  |  |  |

a R Squared $=.988$ (Adjusted R Squared $=.984$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $355.835(\mathrm{a})$ | 9 | 39.537 | 139.510 | .000 |
| Intercept | .064 | 1 | .064 | .228 | .644 |
| trt | 1.696 | 4 | .424 | 1.496 | .275 |
| initialwt | 68.529 | 1 | 68.529 | 241.809 | .000 |
| trt * initialwt | 1.388 | 4 | .347 | 1.225 | .360 |
| Error | 2.834 | 10 | .283 |  |  |
| Total | 19386.950 | 20 |  |  |  |
| Corrected Total | 358.670 | 19 |  |  |  |

a R Squared $=.992$ (Adjusted R Squared $=.985$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $354.447(\mathrm{a})$ | 5 | 70.889 | 235.049 | .000 |
| Intercept | 1.718 | 1 | 1.718 | 5.696 | .032 |
| trt | 12.089 | 4 | 3.022 | 10.021 | .000 |
| initialwt | 156.040 | 1 | 156.040 | 517.384 | .000 |
| Error | 4.222 | 14 | .302 |  |  |
| Total | 19386.950 | 20 |  |  |  |
| Corrected Total | 358.670 | 19 |  |  |  |

a R Squared $=.988$ (Adjusted R Squared $=.984$ )

Parameter Estimates

| Parameter | B | Std. Error | t | Sig. | 95\% Confidence Interval |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Lower Bound | Upper Bound |
| Intercept | 2.495 | 1.028 | 2.427 | . 029 | . 290 | 4.699 |
| [trt=1] | -. 244 | . 577 | -. 424 | . 678 | -1.481 | . 992 |
| [trt=2] | -. 280 | . 493 | -. 569 | . 579 | -1.337 | . 777 |
| [trt=3] | 1.655 | . 429 | 3.853 | . 002 | . 734 | 2.576 |
| [trt=4] | 1.107 | . 472 | 2.347 | . 034 | . 095 | 2.119 |
| [trt=5] | 0(a) |  |  |  | . |  |
| initialwt | 1.083 | . 048 | 22.746 | . 000 | . 981 | 1.185 |

a This parameter is set to zero because it is redundant.

Dependent Variable: Final Weight (g)


Model: Intercept + trt + initialwt

## Q2. Oranges Data : Variety 1 data

Dependent Variable: Quantity Variety 1

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $1346.889(a)$ | 21 | 64.138 | 3.131 | .016 |
| Intercept | 474.876 | 1 | 474.876 | 23.182 | .000 |
| day | 113.659 | 5 | 22.732 | 1.110 | .399 |
| store | 83.136 | 5 | 16.627 | .812 | .561 |
| P1 | 336.892 | 1 | 336.892 | 16.446 | .001 |
| day *P1 | 106.533 | 5 | 21.307 | 1.040 | .432 |
| store *P1 | 82.077 | 5 | 16.415 | .801 | .567 |
| Error | 286.786 | 14 | 20.485 |  |  |
| Total | 5391.693 | 36 |  |  |  |
| Corrected Total | 1633.676 | 35 |  |  |  |

a R Squared $=.824$ (Adjusted R Squared $=.561$ )

Dependent Variable: Quantity Variety 1

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $1264.813(\mathrm{a})$ | 16 | 79.051 | 4.072 | .002 |
| Intercept | 727.513 | 1 | 727.513 | 37.474 | .000 |
| day | 98.792 | 5 | 19.758 | 1.018 | .435 |
| store | 153.290 | 5 | 30.658 | 1.579 | .214 |
| P1 | 488.523 | 1 | 488.523 | 25.164 | .000 |
| day * P1 | 78.987 | 5 | 15.797 | .814 | .555 |
| Error | 368.863 | 19 | 19.414 |  |  |
| Total | 5391.693 | 36 |  |  |  |
| Corrected Total | 1633.676 | 35 |  |  |  |

a R Squared $=.774$ (Adjusted R Squared $=.584$ )

Dependent Variable: Quantity Variety 1

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $1185.825(a)$ | 11 | 107.802 | 5.777 | .000 |
| Intercept | 929.926 | 1 | 929.926 | 49.834 | .000 |
| day | 456.054 | 5 | 91.211 | 4.888 | .003 |
| store | 238.695 | 5 | 47.739 | 2.558 | .054 |
| P1 | 622.008 | 1 | 622.008 | 33.333 | .000 |
| Error | 447.850 | 24 | 18.660 |  |  |
| Total | 5391.693 | 36 |  |  |  |
| Corrected Total | 1633.676 | 35 |  |  |  |

a R Squared = . 726 (Adjusted R Squared $=.600$ )

Dependent Variable: Quantity Variety 1

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $947.131(\mathrm{a})$ | 6 | 157.855 | 6.668 | .000 |
| Intercept | 1094.386 | 1 | 1094.386 | 46.227 | .000 |
| day | 430.538 | 5 | 86.108 | 3.637 | .011 |
| P1 | 696.733 | 1 | 696.733 | 29.430 | .000 |
| Error | 686.545 | 29 | 23.674 |  |  |
| Total | 5391.693 | 36 |  |  |  |
| Corrected Total | 1633.676 | 35 |  |  |  |

a R Squared $=.580$ (Adjusted R Squared $=.493$ )

Dependent Variable: Quantity Variety 1

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $1111.523(a)$ | 11 | 101.048 | 4.644 | .001 |
| Intercept | 854.684 | 1 | 854.684 | 39.284 | .000 |
| P1 | 554.786 | 1 | 554.786 | 25.500 | .000 |
| day | 201.172 | 5 | 40.234 | 1.849 | .141 |
| day *P1 | 164.392 | 5 | 32.878 | 1.511 | .224 |
| Error | 522.153 | 24 | 21.756 |  |  |
| Total | 5391.693 | 36 |  |  |  |
| Corrected Total | 1633.676 | 35 |  |  |  |

a R Squared = . 680 (Adjusted R Squared $=.534$ )

Dependent Variable: Quantity Variety 1

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $516.592(a)$ | 1 | 516.592 | 15.723 | .000 |
| Intercept | 882.193 | 1 | 882.193 | 26.851 | .000 |
| P1 | 516.592 | 1 | 516.592 | 15.723 | .000 |
| Error | 1117.084 | 34 | 32.855 |  |  |
| Total | 5391.693 | 36 |  |  |  |
| Corrected Total | 1633.676 | 35 |  |  |  |

a R Squared $=.316$ (Adjusted R Squared $=.296$ )

## Q2. Oranges Data : Variety 2 data

Dependent Variable: Quantity Variety 2

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $2474.507(\mathrm{a})$ | 21 | 117.834 | 5.984 | .001 |
| Intercept | 856.079 | 1 | 856.079 | 43.471 | .000 |
| store | 189.615 | 5 | 37.923 | 1.926 | .154 |
| day | 321.845 | 5 | 64.369 | 3.269 | .037 |
| P2 | 475.965 | 1 | 475.965 | 24.169 | .000 |
| day *P2 | 277.857 | 5 | 55.571 | 2.822 | .058 |
| store * P2 | 188.695 | 5 | 37.739 | 1.916 | .155 |
| Error | 275.701 | 14 | 19.693 |  |  |
| Total | 7155.720 | 36 |  |  |  |
| Corrected Total | 2750.208 | 35 |  |  |  |

a R Squared $=.900$ (Adjusted R Squared $=.749$ )

Dependent Variable: Quantity Variety 2

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $2285.812(\mathrm{a})$ | 16 | 142.863 | 5.845 | .000 |
| Intercept | 986.830 | 1 | 986.830 | 40.375 | .000 |
| store | 381.265 | 5 | 76.253 | 3.120 | .032 |
| day | 438.673 | 5 | 87.735 | 3.590 | .019 |
| P2 | 587.279 | 1 | 587.279 | 24.028 | .000 |
| day * P2 | 326.468 | 5 | 65.294 | 2.671 | .054 |
| Error | 464.396 | 19 | 24.442 |  |  |
| Total | 7155.720 | 36 |  |  |  |
| Corrected Total | 2750.208 | 35 |  |  |  |

a R Squared $=.831$ (Adjusted R Squared $=.689$ )

Dependent Variable: Quantity Variety 2

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $1959.344(\mathrm{a})$ | 11 | 178.122 | 5.405 | .000 |
| Intercept | 1682.016 | 1 | 1682.016 | 51.043 | .000 |
| store | 309.879 | 5 | 61.976 | 1.881 | .135 |
| day | 773.130 | 5 | 154.626 | 4.692 | .004 |
| P2 | 1001.024 | 1 | 1001.024 | 30.378 | .000 |
| Error | 790.864 | 24 | 32.953 |  |  |
| Total | 7155.720 | 36 |  |  |  |
| Corrected Total | 2750.208 | 35 |  |  |  |

a R Squared $=.712$ (Adjusted R Squared $=.581$ )

Dependent Variable: Quantity Variety 2

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $1649.465(\mathrm{a})$ | 6 | 274.911 | 7.243 | .000 |
| Intercept | 1529.311 | 1 | 1529.311 | 40.291 | .000 |
| day | 763.905 | 5 | 152.781 | 4.025 | .007 |
| P2 | 862.204 | 1 | 862.204 | 22.715 | .000 |
| Error | 1100.743 | 29 | 37.957 |  |  |
| Total | 7155.720 | 36 |  |  |  |
| Corrected Total | 2750.208 | 35 |  |  |  |

a R Squared $=.600$ (Adjusted R Squared $=.517$ )

Dependent Variable: Quantity Variety 2

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $1904.547(a)$ | 11 | 173.141 | 4.914 | .001 |
| Intercept | 894.399 | 1 | 894.399 | 25.383 | .000 |
| day | 371.719 | 5 | 74.344 | 2.110 | .099 |
| P2 | 510.672 | 1 | 510.672 | 14.493 | .001 |
| day *P2 | 255.082 | 5 | 51.016 | 1.448 | .244 |
| Error | 845.661 | 24 | 35.236 |  |  |
| Total | 7155.720 | 36 |  |  |  |
| Corrected Total | 2750.208 | 35 |  |  |  |

a R Squared = . 693 (Adjusted R Squared $=.552$ )

Dependent Variable: Quantity Variety 2

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $885.560(a)$ | 1 | 885.560 | 16.147 | .000 |
| Intercept | 1600.103 | 1 | 1600.103 | 29.176 | .000 |
| P2 | 885.560 | 1 | 885.560 | 16.147 | .000 |
| Error | 1864.648 | 34 | 54.843 |  |  |
| Total | 7155.720 | 36 |  |  |  |
| Corrected Total | 2750.208 | 35 |  |  |  |

a R Squared $=.322$ (Adjusted R Squared $=.302$ )

## Q3. Cotton Data

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $31.361(\mathrm{a})$ | 7 | 4.480 | 106.169 | .000 |
| Intercept | .008 | 1 | .008 | .188 | .667 |
| variety | .057 | 1 | .057 | 1.349 | .252 |
| spacing | .026 | 1 | .026 | .611 | .439 |
| bollwt | 8.210 | 1 | 8.210 | 194.569 | .000 |
| variety * spacing | .003 | 1 | .003 | .075 | .785 |
| variety * bollwt | .328 | 1 | .328 | 7.768 | .008 |
| spacing * bollwt | .001 | 1 | .001 | .014 | .907 |
| variety * spacing * bollwt | $4.13 \mathrm{E}-008$ | 1 | $4.13 \mathrm{E}-008$ | .000 | .999 |
| Error | 1.730 | 41 | .042 |  |  |
| Total | 187.560 | 49 |  |  |  |
| Corrected Total | 33.091 | 48 |  |  |  |

a R Squared $=.948$ (Adjusted R Squared $=.939$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $31.361(\mathrm{a})$ | 6 | 5.227 | 126.884 | .000 |
| Intercept | .009 | 1 | .009 | .221 | .641 |
| variety | .078 | 1 | .078 | 1.889 | .177 |
| spacing | .031 | 1 | .031 | .749 | .392 |
| bollwt | 8.718 | 1 | 8.718 | 211.637 | .000 |
| variety * spacing | .032 | 1 | .032 | .769 | .386 |
| variety * bollwt | .448 | 1 | .448 | 10.881 | .002 |
| spacing * bollwt | .001 | 1 | .001 | .015 | .904 |
| Error | 1.730 | 42 | .041 |  |  |
| Total | 187.560 | 49 |  |  |  |
| Corrected Total | 33.091 | 48 |  |  |  |

a R Squared $=.948$ (Adjusted R Squared $=.940$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $31.360(\mathrm{a})$ | 5 | 6.272 | 155.829 | .000 |
| Intercept | .015 | 1 | .015 | .377 | .542 |
| variety | .091 | 1 | .091 | 2.250 | .141 |
| spacing | .390 | 1 | .390 | 9.691 | .003 |
| bollwt | 11.649 | 1 | 11.649 | 289.413 | .000 |
| variety * spacing | .079 | 1 | .079 | 1.953 | .169 |
| variety * bollwt | .467 | 1 | .467 | 11.606 | .001 |
| Error | 1.731 | 43 | .040 |  |  |
| Total | 187.560 | 49 |  |  |  |
| Corrected Total | 33.091 | 48 |  |  |  |

a R Squared $=.948$ (Adjusted R Squared $=.942$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $31.281(\mathrm{a})$ | 4 | 7.820 | 190.179 | .000 |
| Intercept | .011 | 1 | .011 | .258 | .614 |
| variety | .079 | 1 | .079 | 1.929 | .172 |
| spacing | .375 | 1 | .375 | 9.123 | .004 |
| bollwt | 11.573 | 1 | 11.573 | 281.444 | .000 |
| variety * bollwt | .482 | 1 | .482 | 11.717 | .001 |
| Error | 1.809 | 44 | .041 |  |  |
| Total | 187.560 | 49 |  |  |  |
| Corrected Total | 33.091 | 48 |  |  |  |

a R Squared $=.945$ (Adjusted R Squared $=.940$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $30.906(\mathrm{a})$ | 3 | 10.302 | 212.222 | .000 |
| Intercept | .022 | 1 | .022 | .459 | .502 |
| bollwt | 11.452 | 1 | 11.452 | 235.905 | .000 |
| variety | .109 | 1 | .109 | 2.241 | .141 |
| variety * bollwt | .573 | 1 | .573 | 11.810 | .001 |
| Error | 2.184 | 45 | .049 |  |  |
| Total | 187.560 | 49 |  |  |  |
| Corrected Total | 33.091 | 48 |  |  |  |

a R Squared $=.934$ (Adjusted R Squared $=.930$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $30.799(a)$ | 3 | 10.266 | 201.645 | .000 |
| Intercept | .003 | 1 | .003 | .065 | .800 |
| variety | 1.197 | 1 | 1.197 | 23.517 | .000 |
| spacing | .467 | 1 | .467 | 9.165 | .004 |
| bollwt | 11.572 | 1 | 11.572 | 227.282 | .000 |
| Error | 2.291 | 45 | .051 |  |  |
| Total | 187.560 | 49 |  |  |  |
| Corrected Total | 33.091 | 48 |  |  |  |

a R Squared $=.931$ (Adjusted R Squared $=.926$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $30.333(a)$ | 2 | 15.166 | 252.979 | .000 |
| Intercept | .000 | 1 | .000 | .007 | .934 |
| variety | 1.264 | 1 | 1.264 | 21.076 | .000 |
| bollwt | 11.434 | 1 | 11.434 | 190.724 | .000 |
| Error | 2.758 | 46 | .060 |  |  |
| Total | 187.560 | 49 |  |  |  |
| Corrected Total | 33.091 | 48 |  |  |  |

a R Squared $=.917$ (Adjusted R Squared $=.913$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $29.069(\mathrm{a})$ | 1 | 29.069 | 339.755 | .000 |
| Intercept | .743 | 1 | .743 | 8.689 | .005 |
| bollwt | 29.069 | 1 | 29.069 | 339.755 | .000 |
| Error | 4.021 | 47 | .086 |  |  |
| Total | 187.560 | 49 |  |  |  |
| Corrected Total | 33.091 | 48 |  |  |  |

a R Squared $=.878$ (Adjusted R Squared $=.876$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $31.281(\mathrm{a})$ | 4 | 7.820 | 190.179 | .000 |
| Intercept | .011 | 1 | .011 | .258 | .614 |
| variety | .079 | 1 | .079 | 1.929 | .172 |
| spacing | .375 | 1 | .375 | 9.123 | .004 |
| bollwt | 11.573 | 1 | 11.573 | 281.444 | .000 |
| variety * bollwt | .482 | 1 | .482 | 11.717 | .001 |
| Error | 1.809 | 44 | .041 |  |  |
| Total | 187.560 | 49 |  |  |  |
| Corrected Total | 33.091 | 48 |  |  |  |

a R Squared $=.945$ (Adjusted R Squared $=.940$ )

Parameter Estimates
Dependent Variable: Total Lint Weight (g)

| Parameter | B | Std. Error | t | Sig. | 95\% Confidence Interval |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Lower Bound | Upper Bound |
| Intercept | . 006 | . 125 | . 051 | . 959 | -. 245 | . 258 |
| [variety=37] | -. 312 | . 224 | -1.389 | . 172 | -. 764 | . 141 |
| [variety=213] | 0(a) |  |  |  |  |  |
| [spacing=30] | . 185 | . 061 | 3.020 | . 004 | . 062 | . 308 |
| [spacing=40] | 0(a) |  |  |  | . |  |
| bollwt | . 240 | . 025 | 9.414 | . 000 | . 188 | . 291 |
| [variety=37] * bollwt | . 124 | . 036 | 3.423 | . 001 | . 051 | . 196 |
| [variety=213] * bollwt | O(a) |  |  |  |  |  |

a This parameter is set to zero because it is redundant.

## Dependent Variable: Total Lint Weight (g)



Model: Intercept + variety + spacing + bollwt + bollwt .variety

## Q4: Doses Data

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $994.042(\mathrm{a})$ | 17 | 58.473 | 4.683 | .033 |
| Intercept | 72490.042 | 1 | 72490.042 | 5805.654 | .000 |
| bloc | 538.792 | 3 | 179.597 | 14.384 | .004 |
| type | 12.042 | 1 | 12.042 | .964 | .364 |
| dose | 121.583 | 2 | 60.792 | 4.869 | .055 |
| bloc * type | 47.458 | 3 | 15.819 | 1.267 | .367 |
| bloc * dose | 130.083 | 6 | 21.681 | 1.736 | .260 |
| type * dose | 144.083 | 2 | 72.042 | 5.770 | .040 |
| Error | 74.917 | 6 | 12.486 |  |  |
| Total | 73559.000 | 24 |  |  |  |
| Corrected Total | 1068.958 | 23 |  |  |  |

a R Squared $=.930$ (Adjusted R Squared $=.731$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $946.583(\mathrm{a})$ | 14 | 67.613 | 4.973 | .010 |
| Intercept | 72490.042 | 1 | 72490.042 | 5331.239 | .000 |
| bloc | 538.792 | 3 | 179.597 | 13.208 | .001 |
| type | 12.042 | 1 | 12.042 | .886 | .371 |
| dose | 121.583 | 2 | 60.792 | 4.471 | .045 |
| bloc * dose | 130.083 | 6 | 21.681 | 1.594 | .254 |
| type * dose | 144.083 | 2 | 72.042 | 5.298 | .030 |
| Error | 122.375 | 9 | 13.597 |  |  |
| Total | 73559.000 | 24 |  |  |  |
| Corrected Total | 1068.958 | 23 |  |  |  |

a R Squared $=.886$ (Adjusted R Squared $=.707$ )

Dependent Variable: Response

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $816.500(\mathrm{a})$ | 8 | 102.063 | 6.064 | .001 |
| Intercept | 72490.042 | 1 | 72490.042 | 4307.050 | .000 |
| bloc | 538.792 | 3 | 179.597 | 10.671 | .001 |
| type | 12.042 | 1 | 12.042 | .715 | .411 |
| dose | 121.583 | 2 | 60.792 | 3.612 | .052 |
| type * dose | 144.083 | 2 | 72.042 | 4.280 | .034 |
| Error | 252.458 | 15 | 16.831 |  |  |
| Total | 73559.000 | 24 |  |  |  |
| Corrected Total | 1068.958 | 23 |  |  |  |

a R Squared $=.764$ (Adjusted R Squared $=.638$ )

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $672.417(\mathrm{a})$ | 6 | 112.069 | 4.804 | .005 |
| Intercept | 72490.042 | 1 | 72490.042 | 3107.695 | .000 |
| bloc | 538.792 | 3 | 179.597 | 7.699 | .002 |
| type | 12.042 | 1 | 12.042 | .516 | .482 |
| dose | 121.583 | 2 | 60.792 | 2.606 | .103 |
| Error | 396.542 | 17 | 23.326 |  |  |
| Total | 73559.000 | 24 |  |  |  |
| Corrected Total | 1068.958 | 23 |  |  |  |

a R Squared $=.629$ (Adjusted R Squared $=.498$ )

## Final Model

| Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Corrected Model | $816.500(a)$ | 8 | 102.063 | 6.064 | .001 |
| Intercept | 72490.042 | 1 | 72490.042 | 4307.050 | .000 |
| bloc | 538.792 | 3 | 179.597 | 10.671 | .001 |
| dose | 121.583 | 2 | 60.792 | 3.612 | .052 |
| type | 12.042 | 1 | 12.042 | .715 | .411 |
| dose * type | 144.083 | 2 | 72.042 | 4.280 | .034 |
| Error | 252.458 | 15 | 16.831 |  |  |
| Total | 73559.000 | 24 |  |  |  |
| Corrected Total | 1068.958 | 23 |  |  |  |

a R Squared $=.764$ (Adjusted R Squared $=.638$ )
Parameter Estimates

| Parameter | B | Std. Error | t | Sig. | 95\% Confidence Interval |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Lower Bound | Upper Bound |
| Intercept | 62.042 | 2.512 | 24.696 | . 000 | 56.687 | 67.396 |
| [bloc=1] | 7.667 | 2.369 | 3.237 | . 006 | 2.618 | 12.715 |
| [bloc=2] | -3.500 | 2.369 | -1.478 | . 160 | -8.549 | 1.549 |
| [bloc=3] | -4.333 | 2.369 | -1.830 | . 087 | -9.382 | . 715 |
| [bloc=4] | 0(a) |  |  | . | . |  |
| [dose=1] | -11.250 | 2.901 | -3.878 | . 001 | -17.433 | -5.067 |
| [dose=10] | -7.750 | 2.901 | -2.672 | . 017 | -13.933 | -1.567 |
| [dose=100] | 0(a) | . |  | . |  |  |
| [type=1] | -8.000 | 2.901 | -2.758 | . 015 | -14.183 | -1.817 |
| [type=2] | 0(a) |  |  | . | . |  |
| [dose=1] * [type=1] | 11.750 | 4.103 | 2.864 | . 012 | 3.006 | 20.494 |
| [dose=1] * [type=2] | O(a) |  |  | . | . |  |
| [dose=10] * [type=1] | 8.000 | 4.103 | 1.950 | . 070 | -. 744 | 16.744 |
| [dose=10] * [type=2] | 0(a) | . |  | . | . |  |
| [dose=100] * [type=1] | O(a) |  |  | . |  |  |
| [dose=100] * [type=2] | O(a) | . |  | . | . |  |

a This parameter is set to zero because it is redundant.

## Dependent Variable: Response



Model: Intercept + bloc + dose + type + dose * type

