

Lecture 1

- Introduction to arithmetic fundamental groups and path torsors.
- Galois actions. Grothendieck's section conjecture.
- Unipotent completions and Lie algebras. Galois actions and periods on unipotent completions.

Supplementary lecture: Romyar Sharifi (Galois actions on fundamental groups, Ihara theory)

Lecture 2

- Non-abelian cohomology and construction of classifying spaces for torsors.
- The crystalline condition on local torsors.
- De Rham/crystalline fundamental group and path torsors.
- Construction of De Rham/crystalline classifying space.

Supplementary lecture: Amnon Besser (Conceptual approach to Coleman integration.)

Lecture 3

- p-adic Hodge theory and comparison isomorphisms.
- Computation of the local unipotent Albanese map and p-adic multiple polylogarithms.

Supplementary lecture: Bryden Cais (Comparison isomorphisms and Bloch-Kato log/exponential in the abelian case.)

Lecture 4

- Finiteness theorems I
- Projective line minus 3 points.
- Elliptic curves with CM.
- Curves with CM Jacobian.

Supplementary lecture: Henri Darmon (Iwasawa theory and p-adic L-functions.)

Lecture 5

- Finiteness theorems II
- Projective line minus three points over totally real field.
- Elliptic curve minus one point.
- Speculations on non-abelian duality.

Supplementary lecture: Jennifer Balakrishnan (Computational theory of iterated Coleman integration.)